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A FINITE DIFFERENCE PROGRAM FOR COMPUTING THE THERMO-ELASTIC-PLASTIC RESPONSE OF LINED GUN BARRELS

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A finite difference computer program for computing the thermo-elastic-plastic response of multi-layered cylinders due to repeated firing loads was discussed at the 27th Conference of Army Mathematicians. The multi-layered cylinder is a representation of a lined gun barrel. The program can accommodate several layers and can compute the transient temperatures and/or the stresses. It has been upgraded to include an initial program which computes heat transfer (CONT'D ON REVERSE)

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INTRODUCTION

This report describes a finite difference computer program for investigating the response of multilayered gun barrels subject to some firing cycle. Results, typical of which the program is capable of generating, are presented for a tube model which has a TZM liner and a steel jacket. The application is to a large caliber weapon, but the program can be used for small caliber also. The program was written to coincide with a development program which is examining the feasibility of fabricating and firing multilayered gun tubes. One of the main factors limiting the life of gun tubes is the excessive wear and erosion which occurs especially at the forcing cone area of the gun tube. The experimental program, which has shown success for 20 mm weapons, is to insert liners fabricated from refractory materials into the forcing cone area of the gun tube. Since refractory materials have high melting points, there is a strong indication that they will experience less wear and thus increase the life of the weapon.

Earlier versions of the computer program have been used to describe other behavior. 1-3 Preliminary work on the current problem was presented in reference 3. That work has been improved by inputting the thermo-physical properties as functions of temperature and by allowing contact resistance

l Vasilakis, J. D., "Temperatures and Stresses Due to Quenching of Hollow Cylinders," Transactions of the 24th Conference of Army Mathematicians, ARO Report 79-1, January 1979.

²Vasilakis, J. D. and Chen, P. C. T., "Thermo-Elastic-Plastic Stresses on Hollow Cylinders Due to Quenching," Transactions of the 25th Conference of Army Mathematicians, ARO Report 80-1, January 1980.

³ Vasilakis, J. D., "Thermo-Elastic Plastic Stresses in Multi-Layered Cylinders," Transactions of the 27th Conference of Army Mathematicians, ARO Report 82-1, January 1982.

now generated for the current problem at hand, i.e., for specific configuration and bore material, whereas previously they were empirically generated for another system and simply used in the program as typical input.

The computer program consists of three parts which can be run as a single program or as three separate stand alone programs. The first is an internal ballistics program which generates the boundary conditions, i.e., heat transfer coefficients, pressures, and gas temperatures as a function of time for a single firing pulse, for input to the next two programs. The next program section computes the transient temperatures due to some firing cycle and can be used to show the thermal response of the system over several firing cycles indicating the temperature buildup, and/or the temperatures can be used as input to the third program section for the computation of stresses. This can be done as the thermo-mechanical program is treated as uncoupled.

Results from each of the three sections using a TZM liner/steel jacket configuration for a 105 mm large caliber weapon system are presented.

PROCEDURE

The equations used to describe the behavior are discussed below followed by the numerical work.

Theory

The partial differential equation for describing the axisymmetric transient temperature distribution in multilayered cylinders is given by, for layer L,

$$\frac{1}{r} \frac{\partial}{\partial r} \left(k^{L}(T) r \frac{\partial T^{L}}{\partial r} \right) = c^{L}(T) \rho^{L}(T) \frac{\partial T^{L}}{\partial t}$$
 (1)

where r represents the radial distance, T the temperature, and t the time. The thermal conductivity, specific heat, and density are given by k, c, and ρ respectively. These properties are assumed to be functions of temperature. Axial effects are ignored in the program. The geometry is shown in Figure 1.

The initial condition is given by

$$T(r,o) = T_0 \tag{2}$$

where T_0 would normally represent some ambient temperature. A temperature other than ambient, say due to some environmental condition, could also be used. The boundary conditions are of the type

$$k(T) \frac{\partial T}{\partial r} - h(T - T_g) = -g$$
 (3)

where h is convection type heat transfer coefficient, g would represent some heat input if it existed, and Tg is the temperature of the propellant gases when the boundary condition is applied on the inside or bore diameter and the ambient temperature when applied on the outside surface of the gun tube.

The thermo-physical properties are made dimensionless with regard to their respective values for steel at the ambient temperature. The temperatures are made dimensionless with regard to the maximum gas temperature achieved during the interior ballistic cycle. The dimensionless time is defined by

$$\tau = \frac{k_0 t}{\rho_0 c_0 b^2} \tag{4}$$

where k_0 , ρ_0 , and c_0 are the values for steel as mentioned previously. In the boundary conditions,

$$\hat{h} = \frac{hb}{k} \tag{5}$$

becomes the Nusselt number.

Also required are continuity conditions between the concentric cylinders. Normally one requires continuity of temperature and heat flux. However, contact resistance does exist between surfaces and it was decided to include this effect here. The resistance results from the true nature of surfaces. 4 Conduction occurs at the discrete points of contact between the surfaces and is therefore a function of pressure, surface conditions, fluids in the voids, etc. It is treated here as a thin layer resisting the flow of heat. For the finite difference formulation, there is a jump in temperature at node i

$$T_i^{L} = T_i^{L+1} + \Delta T \tag{6}$$

while the heat flux

$$\frac{q}{A} = k^{L}(T) \frac{T_{i-1}^{L} - T_{i}^{L}}{\Delta r} = h_{c}\Delta T = k^{L+1}(T) \frac{T_{i}^{L+1} - T_{i+1}^{L+1}}{\Delta r} .$$
 (7)

remains constant as one passes across the layer from cylinder L to cylinder L+1. Equations (6) and (7) allow the computation of ΔT and T_1^{L+1} .

The use of finite difference equations to solve the thermo-elasticplastic stress problem requires expressing the equilibrium equation and the
equation of compatibility at each node at which the finite difference
equations are desired. The Prandtl-Reuss flow rule is used to eliminate the
incremental stresses so that what results is a matrix for evaluating the
incremental radial and tangential strains at each node. The required
equations follow, written in dimensionless form. The problem is treated as
plane strain.

⁴Fenech, H. and Rohsenow, W. M., "Prediction of Thermal Conductance of Metallic Surfaces in Contact," Journal of Heat Transfer, February 1963, pp. 15-24.

The equation of equilibrium is written

$$\frac{\partial \sigma_{\mathbf{r}}}{\partial \mathbf{r}} + \frac{\sigma_{\mathbf{r}} - \sigma_{\theta}}{\mathbf{r}} = 0 \tag{8}$$

where

$$\sigma_{r} = \frac{\sigma_{r}}{\sigma_{0}}$$
 is the dimensionless radial stress

$$\sigma_{\theta} \ (= \frac{\sigma_{\theta}}{\sigma_{0}})$$
 is the dimensionless tangential stress

and σ_0 is the yield stress in tension, and the compatibility equation

$$\frac{\partial \varepsilon_{\theta}}{\partial r} + \frac{\varepsilon_{\theta} - \varepsilon_{r}}{r} = 0 \tag{9}$$

where

$$\epsilon_{\theta}$$
 . $\epsilon_{\theta}(=$ E $\stackrel{--}{--})$ is dimensionless tangential strain σ_{0}

$$\varepsilon_{\mathbf{r}} (= \mathbf{E} \frac{\varepsilon_{\mathbf{r}}}{-})$$
 is dimensionless radial strain

and σ_0/E is yield strain in tension when E is Young's Modulus. The compressibility of the material is expressed by

$$\varepsilon = \alpha T + \frac{\sigma}{3K}$$

$$\varepsilon = \frac{1}{3} (\varepsilon_r + \varepsilon_\theta) \text{ is mean strain}$$

$$\sigma = \frac{1}{3} (\sigma_r + \sigma_\theta + \sigma_z) \text{ is mean stress}$$

$$K(=\frac{K}{\sigma_0})$$
 is dimensionless bulk modulus

 α (= αT_1) is dimensionless coefficient of thermal expansion

and

$\varepsilon_z = 0$ for plane strain

Traction free boundary conditions are always used in the outside radius and on the bore when only thermal stresses are required. When mechanical loads are desired, the pressure pulse is applied to the bore.

It was desirable to write the finite difference equations in terms of strain alone; hence, the stresses in the equations of equilibrium had to be expressed in terms of the strains. This was accomplished by modifying a plastic stress-strain matrix⁵ which was derived by inverting the Prandtl-Reuss equations. The inverted Prandtl-Reuss equation is

$$\{d\sigma\} = [D^{P}]\{d\epsilon\} - \frac{E\alpha dT}{(1-2\nu)\sigma_{0}} \{1\}$$
 (11)

where the stress vector is $\{d\sigma\} = \{d\sigma_r, d\sigma_\theta, d\sigma_z\}^T$, the strain vector $\{d\epsilon\} = \{d\epsilon_r, d\epsilon_\theta, 0\}^T$, and $\{1\}$ represents a unit vector. The plastic stress-strain matrix $[D^P]$ is given by

$$[D^{P}] = \frac{1}{1+\nu} \begin{bmatrix} \frac{1-\nu}{1-2\nu} & \frac{\sigma_{\mathbf{r}}^{\dagger 2}}{S} \\ \frac{\nu}{1-2\nu} & \frac{\sigma_{\mathbf{r}}^{\dagger} \sigma_{\theta}^{\dagger}}{S} & \frac{1-\nu}{1-2\nu} & \frac{\sigma_{\theta}^{\dagger 2}}{S} \\ \frac{\nu}{1-2\nu} & \frac{\sigma_{\mathbf{r}}^{\dagger} \sigma_{\mathbf{z}}^{\dagger}}{S} & \frac{\nu}{1-2\nu} & \frac{\sigma_{\theta}^{\dagger} \sigma_{\mathbf{z}}^{\dagger}}{S} & \frac{1-\nu}{1-2\nu} & \frac{\sigma_{\mathbf{z}}^{\dagger 2}}{S} \end{bmatrix}$$
(12)

⁵Yamada, Y., Yoshimura, N., and Sakuri, T., "Plastic Stress-Strain Matrix and Its Application For the Solution of Elastic-Plastic Problems by the Finite Element Method," International Journal of Mechanical Sciences, 1968, Vol. 10, pp. 343-354.

The primed stresses are deviatoric stresses,

$$\sigma_{\mathbf{i}}' = \sigma_{\mathbf{i}} - \frac{1}{3} \sum_{i=1}^{\infty} \sigma_{\mathbf{i}} \quad i = r, \theta, z$$
 (13)

At each node during a computation, the von Mises' yield criterion

$$\frac{1}{2} [(\sigma_{r} - \sigma_{\theta})^{2} + (\sigma_{\theta} - \sigma_{r})^{2} + (\sigma_{z} - \sigma_{r})^{2}] = 1$$
 (14)

is checked to see if plastic deformation has progressed to that node. If not the stresses remain elastic and can still be computed using Eq. (12) by setting the deviatoric stresses equal to zero. The matrix $[D^P]$ then becomes the same matrix as would exist if linear elastic behavior had been assumed. The quantity S is given by

$$S = \frac{2}{3} \sigma^2 \left(1 + \frac{H'}{3G}\right) \tag{15}$$

where

$$\overline{\sigma} = \frac{3}{2} \sigma_{ij}' \sigma_{ij} = \frac{3}{2} (\sigma_r'^2 \sigma_{\theta'}^2 \sigma_z^2)$$
 (16)

is the equivalent stress and

$$H' = \frac{d\sigma}{d\varepsilon_{p}} \tag{17}$$

is the slope of the equivalent stress/equivalent plastic strain curve and is a measure of hardening. The increment in equivalent plastic strain is given by

$$\frac{1}{d\varepsilon_{p}} = \frac{2}{3} d\varepsilon_{ij} p d\varepsilon_{ij} p$$
(18)

Boundary Conditions

The boundary conditions that are used as input for the calculation of temperatures and of stresses are generated using a computer program based on reference 6. In that paper, the burning of a specific propellant for the purpose of firing a projectile from a gun tube is modeled. The equations used are based on Corner's work⁷ and represent a first order interior ballistics solution. Lagrange's approximation is assumed, i.e., the velocity of the gas at any instant increases linearly with distance along the bore from zero at the breech to the full shot velocity at the base of the projectile. Exponential decay is assumed during the blowdown cycle, i.e., after the projectile has left the gun tube. Based upon the rate equations and heat balances involved, the heat transfer coefficients, the pressure pulse, and the gas temperature can be found as a function of time during the firing cycle. The quantity of heat that goes into the heating of the gun tube can be computed. The bore surface can be specified to be the liner material. Figure 2 shows the output of this program for a gun tube with steel at the bore surface.

Numerical Procedure

The Crank-Nicolson representation for finite differences of the partial differential equation governing the temperatures in time is $^{\rm l}$

¹ Vasilakis, J. D., "Temperatures and Stresses Due to Quenching of Hollow Cylinders," Transactions of the 24th Conference of Army Mathematicians, ARO Report 79-1, January 1979.

⁶Vottis, P. M., "Digital Computer Simulation of the Interior Ballistic Process in Guns," WVT-6615, Watervliet Arsenal, Watervliet, NY, October 1966.

⁷Corner, J., <u>Theory of Interior Ballistics of Guns</u>, John Wiley and Sons, Inc., New York, 1950.

$$[a+i\Delta r)k_{i+1/2,n+1/2}]T_{i+1,n+1} + [-(a+i\Delta r)k_{i+1/2,n+1/2} \\ -(a+(i-1)\Delta r)k_{i-1/2,n+1/2}\rho_{i,n+1/2}(\frac{2\Delta r^{2}}{-\Delta t})(a+(i-1/2)\Delta r)T_{i,n+1} \\ + [(a+(i-1)\Delta r)k_{i-1/2,n+1/2}]T_{i-1,n+1} = [-(a+i\Delta r)k_{i+1/2,n+1/2}]T_{i+1,n} + \\ + [(a+i\Delta r)k_{i+1/2,n+1/2} + (a+(i-1)\Delta r)k_{i-1/2,n+1/2} - \\ c_{i,n+1/2}\rho_{i,n+1/2}(\frac{2\Delta r^{2}}{-\Delta t})(a+(i-1/2)\Delta r)]T_{i,n} + [-(a+(i-1)\Delta r)k_{i-1/2,n+1/2}]T_{i-1,n}$$

$$(19)$$

The equation is solved twice:

- 1. At n+1/2 step, allowing k,ρ,c etc. to take on the values at t=n step.
- 2. The new temperatures are then used to evaluate k,c,ρ at n+1/2 step and the set of equations re-evaulated for the temperatures at the n+1 step.

The computed temperature distributions at each full-time step are saved on disk and eventually called in when required by the stress program.

The finite difference equations are within any layer.

Compatibility:

$$-\mathbf{r}_{\mathbf{i}}\Delta\varepsilon_{\theta} + (2\mathbf{r}_{\mathbf{i}}-\mathbf{r}_{\mathbf{i}-1})\Delta\varepsilon_{\theta} - (\mathbf{r}_{\mathbf{i}}-\mathbf{r}_{\mathbf{i}-1})\Delta\varepsilon_{\mathbf{r}_{\mathbf{i}}} = \\
-\mathbf{r}_{\mathbf{i}}(\varepsilon_{\theta} - \varepsilon_{\theta}) - (\mathbf{r}_{\mathbf{i}}-\mathbf{r}_{\mathbf{i}-1})(\varepsilon_{\theta} - \varepsilon_{\theta})$$
(20)

Equilibrium:

$$-r_{i} \Delta \sigma_{r_{i-1}} - (r_{i} - r_{i-1}) \Delta \sigma_{\theta_{i}} + (2r_{i} - r_{i-1}) \Delta \sigma_{r_{i}} - r_{i} (\sigma_{r_{i}} - \sigma_{r_{i-1}}) - (r_{i} - r_{i-1}) (\sigma_{r_{i}} - \sigma_{\theta_{i}})$$
(21)

Substituting the Prandtl-Reuss equations into that of equilibrium

$$-r_{i}D(r,\theta)\Delta\varepsilon_{\theta_{i-1}} -r_{i}D(r,r)\Delta\varepsilon_{r_{i-1}} + [-(r_{i}-r_{i-1})D(\theta,\theta) + (2r_{i}-r_{i-1})D(r,\theta)]\Delta\varepsilon_{\theta_{i}}$$

$$+ [-(r_{i}-r_{i-1})D(\theta,r) + (2r_{i}-r_{i-1})D(r,r)]\Delta\varepsilon_{r_{i}}$$

$$r_{i}[\sigma_{r_{i-1}}-\sigma_{r_{i}}] + (r_{i}-r_{i-1})(\sigma_{\theta_{i}}-\sigma_{r_{i}}) + r_{i}\frac{E\alpha}{1-2\nu} [\Delta T_{i}-\Delta T_{i-1}] \qquad (22)$$

Equations (20) and (21) are in backward difference equations. The actual computations are performed by averaging backward and forward difference schemes. At the interface between cylinders, continuity of the radial stress and radial displacement is specified and on the boundary, i = 1,

$$D(r,\theta)\Delta\varepsilon_{\theta} + D(r,r)\Delta\varepsilon_{r} = \frac{E\alpha\Delta T_{1}}{1-2\nu} - \Delta p_{1}$$
 (23)

where Δp_1 represents a pressure increment at the bore or inside diameter.

The solution procedure for the transient temperature problem is as follows. The temperature problem is solved, and the temperature distributions at their computation times are stored on disk. These distributions are called into the thermo-elastic-plastic stress program one at a time. The corresponding thermal stresses are calculated and each node checked to see if the yield criterion is satisfied. If not, the problem is still assumed to be elastic, a new temperature distribution is called in, and new stress increments calculated. The stresses are updated, and the yield criterion checked again. When the stresses at a point are found to satisfy the yield criterion, the node is identified, and the stress increments at that node from the next set of temperatures are computed using the Prandtl-Reuss equation or [DP] matrix identified earlier. This procedure is continued with new sets of temperature called in and with the tracking of the elastic-plastic boundary with time.

The mechanical properties are evaluated at the existing temperatures. However, the yield stress has not yet been incorporated as a function of temperature in the program.

Mechanical and Thermo-Physical Properties

The properties used in the calculations were found in reference 8. The nominal values are given in Table I. It is always one of the more difficult tasks to find properties as functions of temperature. The steel properties used were those of 4340 and 4150. "Gun Steel" is typically 4340 or a modification thereof. The thermo-physical properties for TZM used were those for molybdenum itself since they were readily available as functions of temperature and the same properties for TZM, only given at one or two specified temperatures tended to fall on or near the same property for molybdenum.

TABLE I. ROOM TEMPERATURE PROPERTIES

	k	С	ρ	α	Е	σур	ν
	BTU/#in°F	BTU/#°F	#/in ³	in/in°F	Psi	Psi	
Steel	5.01x10-4	.105	•289	6.2x10 ⁻⁶	30x10 ⁶	160x10 ³	.3
TZM	1.87x10 ⁻⁴	•06	•369	3.0x10 ⁶	45x10 ⁶	130x10 ³	•314

⁸Aerospace Structural Metals Handbook, AFML-TR-68-115.

RESULTS

The interior ballistic code was first run to set up the input data (heat transfer for coefficients and gas temperatures during firing cycle) for the position of the program which computes the transient temperature distribution and pressure time curve for the mechanical load contribution to the stress part of the program. Two data sets were established, one for steel at the bore and one for TZM at the bore. Figure 2 shows the results for steel. The interior ballistic code computes these results at several stations along the tube, but only the section at which the maximum pressure was generated was considered at this time. The temperature portion of the program serves two separate purposes. The program can be run over several firing pulses based on some specific firing cycle. This will show the buildup in temperature during the firing. It can also be run to provide input data in the form of temperature distributions throughout the wall of the tube for specific times during the firing cycle. This data set is then used in the stress program for the computation of thermal stresses or thermo-mechanical stresses when the pressure-time curve is also applied. There were four types of material problems considered, a single (monobloc) steel tube with constant properties, monobloc steel tube with temperature dependent properties, a TZM liner/steel jacket with constant properties in each cylinder, and a TZM liner/steel jacket with temperature dependent properties. Results from some of these cases are presented below.

Figure 3 shows the change of the bore temperature with time over four firing cycles. The configuration is the TZM liner/steel jacket with temperature dependent properties. The firing cycle depicted represents a projectile being fired at the rate of four rounds per minute. The temperature buildup at

the bore can easily be seen. Figure 4 shows the temperature response at the bore for a monobloc steel tube with temperature dependent properties. This is shown on an expanded scale and represents the thermal response used on one of the data sets for the stresses. When these data sets for stresses are established, a finer time increment is used over that which simply computes the thermal response for temperature buildup. The finer time increment decreases the temperature difference, ΔT , from time step to time step which is used in the stress program. This helps in approaching yield in the stress program even though the temperature difference is further divided near yielding and after yielding has begun. When only the temperatures themselves are desired, it was previously shown that larger time increments can be used. As the finite difference program for temperatures is implicit, the time increment between pulses is increased at a rapid rate until the next firing pulse comes along. It took approximately 90 time steps to complete the temperature response to the four cycles.

When investigating the effect of contact resistance, it becomes obvious why many papers ignore it. The difficulty is not with the computation, but rather the uncertainty of the physical constant to use in the evaluation. The property h described earlier, is treated as a constant here but in reality would be a function of pressure, temperature, the roughness of the surfaces in contact, the hardness of the materials involved, etc. One would actually need the true area of contact as opposed to the apparent area and how this changed

³Vasilakis, J. D., "Thermo-Elastic-Plastic Stresses in Multi-Layered Cylinders," Transactions of the 27th Conference of Army Mathematicians, ARO Report 82-1, January 1982.

in time. Table II shows the effect of varying h on the bore temperature for five firing pulses. The h is dimensionless. The table shows that when h = 1000, the system is equivalent to having no resistance to heat flow and when h = .00001, the effect is equivalent to zero heat flow at the interface. As can be seen by converting some of the values from reference 4, one can get coefficients which result in measurable effects. To better show the effect, the resulting temperature distribution as a function of radius as shown in Figure 5 for h = 1. The second, third, and fourth pulses are displaced from the first for clarity of viewing. The bore temperature increases substantially compared to zero contact resistance (as can also be seen from Table II). The temperature jump also increases substantially. The line indicating the jump should be a vertical line from the point on the inner cylinder. The fact that it is not is due to the plotting routine. A final remark on this section would be that with the uncertainty in computing or experimentally determining an actual h for a system, Table II shows little difference between an h = 1000 and h = 100 as a threshold for zero contact resistance and again little difference between h = .1 and h = .00001 for an insulating barrier.

⁴Fenech, H. and Rohsenow, W. M., "Prediction of Thermal Conductance of Metallic Surfaces in Contact," Journal of Heat Transfer, February 1963, pp. 15-24.

TABLE II. EFFECT OF H ON BORE TEMPERATURE

		1000	100	1	.1	•00001
	Pulse l	0	0	0	0	0
	Pulse 2	.00352	.00356	.00837	.00999	.01021
Temp	Pulse 3	•00580	.00582	.01493	.01952	.02020
	Pulse 4	•00758	.00756	.02013	.02861	.02998
	Pulse 5	•00904	•00901	•02424	.03728	.03596

The remaining results relate to the output from the stress portion of the program. Figure 6 shows the effect of including temperature dependence of material properties in the analysis. The variation of radial stress and tangential stress across the wall thickness is shown. There is little effect except at the peak tangential stress at the bore which is about three to four percent higher for a tube with temperature dependent material properties. This represents a stress difference of about 5000 psi.

The stress results being shown are only the response to the first firing pulse. Hence, the stresses are mainly due to a steep thermal gradient at the bore of the tube. If inelastic response does not occur, the stress response would not change significantly from pulse to pulse as the mechanical load vanishes and there remains only a slight thermal gradient throughout the tube wall. Depending on the configuration of the system, the firing rate, etc., the rise in bore temperature before the next round is fired is small, ~ 3°F to 9°F.

Figure 7 shows the variation in tangential stress versus radius for the multi-cylinder configuration, TZM/steel, with the temperature dependent properties at the time when the internal pressure peaks. The mechanical loading due to the pressure-time curve alone is shown as is the thermal stress distribution due to the temperature distribution. The combined effects are also shown.

These combined effects are not arrived at by adding the separate ones but are recomputed. This is important, especially in the case shown, because the mechanical load alone was sufficient to cause the inelastic deformation at the bore. While this inelastic zone was concentrated at the bore and there was little depth of plastic zone penetration into the wall, it was still incorrect to linearly superimpose solutions by adding the separate stress distributions. Under the combined loads, the solution remained elastic throughout. Figure 8 shows the results from the same problem at peak thermal load.

SUMMARY

The computer program described is capable of predicting the thermal response and the thermo-elastic-plastic response of liner/jacket gun tube designs with temperature dependent thermo-physical properties. Realistic input to this problem is generated using an interior ballistics code. While only a two cylinder system is described, allowance is made for up to five cylinders.

Improvements can always be made and in this case, the following could be included. By using a variable space increment in the thermal program, the effect of a deposited thin layer on the bore surface can be investigated. Initial stresses due to interference should be incorporated as should a temperature dependent yield stress.

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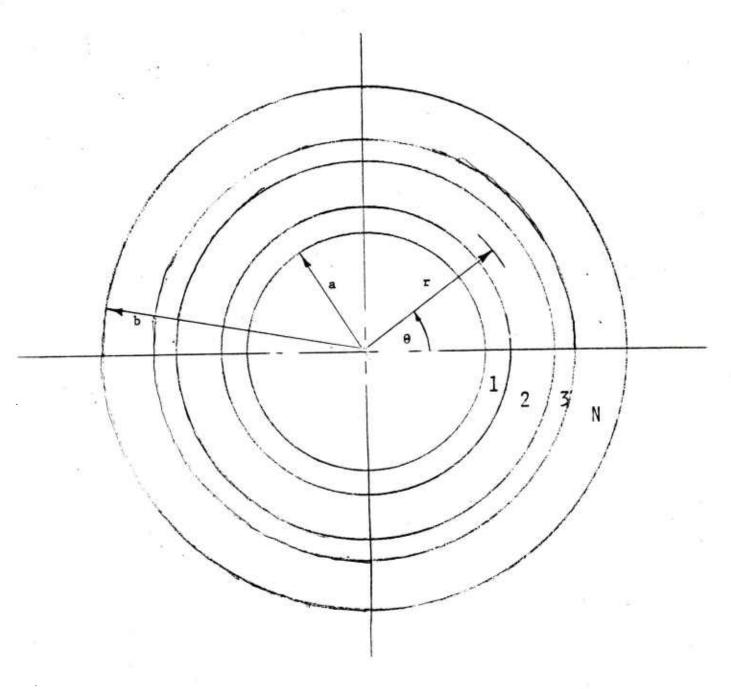
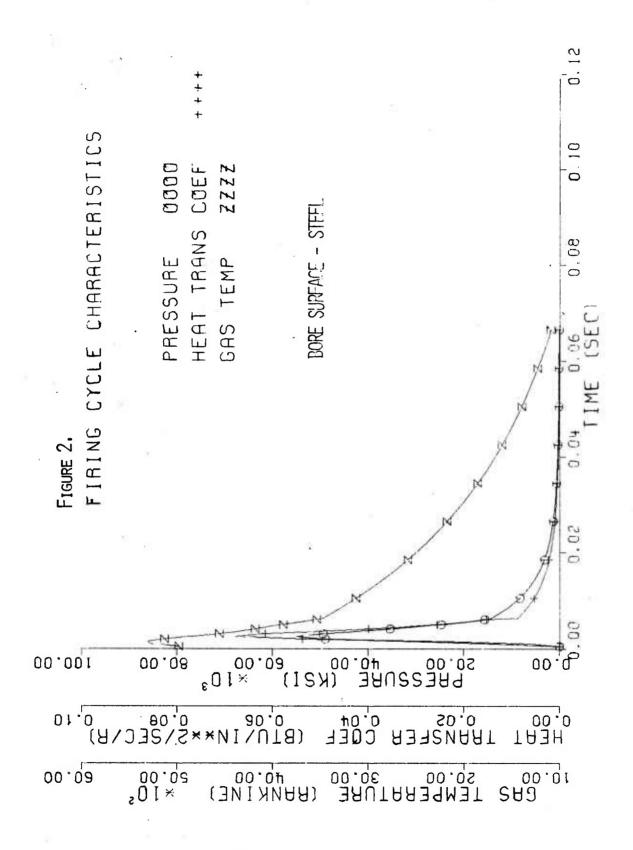


FIGURE 1. TYPICAL MULTI-LAYERED GEOMETRY



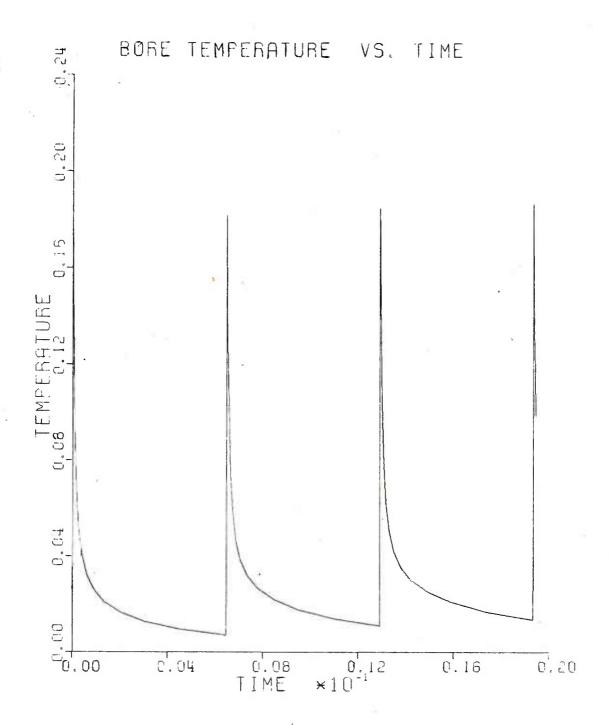


FIGURE 3. BORE TEMPERATURE RESPONSE OVER SEVERAL FIRING CYCLES.

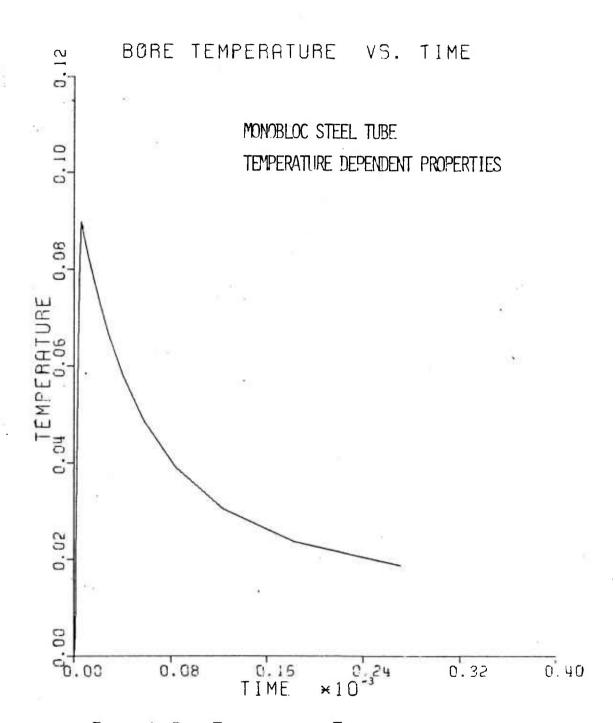


FIGURE 4. BORE TEMPERATURE VS TIME.

RESPONSE FOR INPUT TO STRESS PROGRAM.

FIGURE 5, TEMPERSTURE VS RADIUS

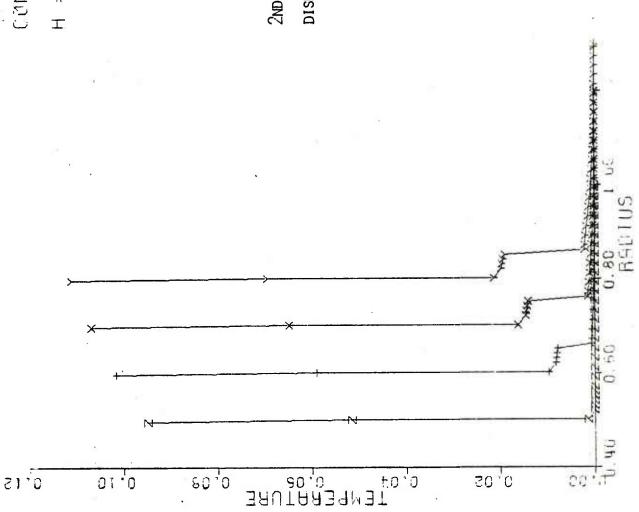
EFFECTS	-
RESISTANCE	
CONTACT	

H = 1.0 IST PULSE 2ND PULSE ..

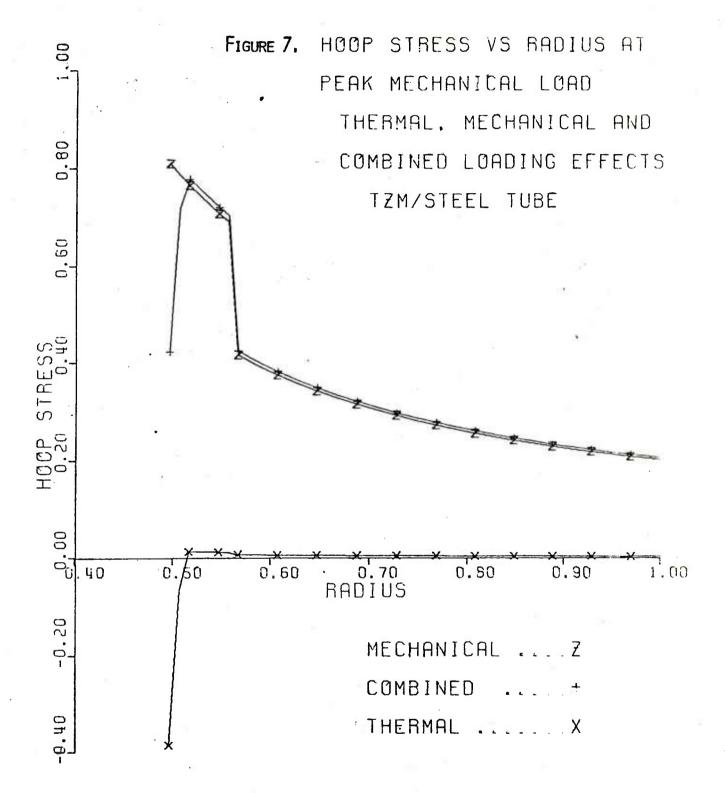
3RU PULSE

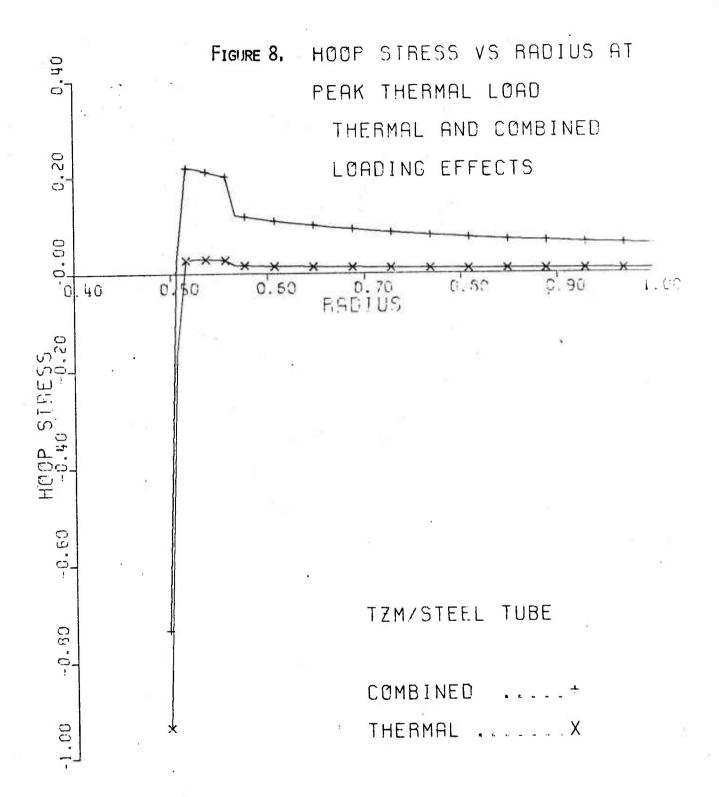
4TH PULSE ..

2ND, 3RD AND HTH PULSE ARE DISPLACED FROM 1ST FOR VIEWING



TUBE DEPENDENCE STEEL RADIAL (T=CONST) RADIAL (FUNC (T) HOOP (T=CONST) HOOP (FUNC (T)) RADIUS FOR TEMPERATURE STRESS VS EFFECTS FIGURE 6. 00 · 6 09.0os.co 218ESS -0.40 09.0-





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